Bilkent University
Quiz \# 03
Math 101-Section 12 Calculus I
20 October 2022 Thursday
Instructor: Ali Sinan Sertöz

## Solution Key

Q-1) The sides $x$ and $y$ of a right triangle are changing as functions of time. When $x=3$ and $y=4$, we observe that $x^{\prime}=2, y^{\prime}=1, x^{\prime \prime}=-4$ and $y^{\prime \prime}=-2$. Denoting the hypothenuse of this triangle by $h$,
(a) find $h^{\prime}$ at that given time,
(b) find $h^{\prime \prime}$ at that given time.

Show your work in detail. Correct answers without detailed explanation do not get any credit.
Grading: $5+5=10$ points.
Solution: Our basic equation is

$$
\begin{equation*}
h^{2}=x^{2}+y^{2} . \tag{1}
\end{equation*}
$$

Differentiating both sides of this equation with respect to time, and dividing by 2 , we get

$$
\begin{equation*}
h h^{\prime}=x x^{\prime}+y y^{\prime} . \tag{2}
\end{equation*}
$$

Differentiating once more we get

$$
\begin{equation*}
\left(h^{\prime}\right)^{2}+h h^{\prime \prime}=\left(x^{\prime}\right)^{2}+x x^{\prime \prime}+\left(y^{\prime}\right)^{2}+y y^{\prime \prime} . \tag{3}
\end{equation*}
$$

Putting $x=3, y=4$ into (1) we get $h=5$. Now solving (2) we get $h^{\prime}=2$.
Putting these into (3) and solving we get $h^{\prime \prime}=-\frac{19}{5}$.

