NAME:....

## Ali Sinan Sertöz

STUDENT NO:....

## Math 113 Calculus – Homework 1

| 1  | 2  | 3  | 4  | TOTAL |
|----|----|----|----|-------|
|    |    |    |    |       |
|    |    |    |    |       |
|    |    |    |    |       |
| 25 | 25 | 25 | 25 | 100   |

*Please do not write anything inside the above boxes!* 

Check that there are 4 questions on your booklet. Write your name on top of every page. Show your work in reasonable detail. A correct answer without proper or too much reasoning may not get any credit.

**Q-1**) Consider the function  $f(x) = \frac{1}{x}$  for x > 0.

For each given  $\epsilon > 0$  and for each  $x_0 > 0$ , find explicitly a  $\delta > 0$  (which usually depends both on  $\epsilon$  and  $x_0$ ) such that for all x > 0 with  $|x - x_0| < \delta$  we will have  $|f(x) - f(x_0)| < \epsilon$ .

**Q-2**) Consider the function  $f(x) = \frac{1}{x}$  for x > 0.

Prove or disprove that given any  $\epsilon > 0$ , there exists a  $\delta > 0$  (which depends only on  $\epsilon$ ) such that for all x, y > 0 with  $|x - y| < \delta$  we will have  $|f(x) - f(y)| < \epsilon$ .

**Q-3**) Consider the function  $f(x) = \frac{1}{x}$  for  $x \in [1, 5]$ .

Prove or disprove that given any  $\epsilon > 0$ , there exists a  $\delta > 0$  (which depends only on  $\epsilon$ ) such that for all  $x, y \in [1, 5]$  with  $|x - y| < \delta$  we will have  $|f(x) - f(y)| < \epsilon$ .

**Q-4)** Consider the function  $f(x) = \frac{1}{x}$  for  $x \in [1, \infty)$ .

Prove or disprove that given any  $\epsilon > 0$ , there exists a  $\delta > 0$  (which depends only on  $\epsilon$ ) such that for all  $x, y \in [1, \infty)$  with  $|x - y| < \delta$  we will have  $|f(x) - f(y)| < \epsilon$ .