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## Math 114 Calculus - Homework 4

| 1 | 2 | 3 | 4 | TOTAL |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
|  |  |  |  |  |
| 25 | 25 | 25 | 25 | 100 |

Please do not write anything inside the above boxes!
Check that there are 4 questions on your booklet. Write your name on top of every page. Show your work in reasonable detail. A correct answer without proper or too much reasoning may not get any credit.

Q-1) Find the following sums

$$
\sum_{n=0}^{\infty} \frac{n^{3}}{2^{n}} \quad \text { and } \quad \sum_{n=0}^{\infty}(-1)^{n} \frac{n^{3}}{2^{n}}
$$

## Solution:

Q-2) Find the following limit.

$$
\lim _{x \rightarrow 0} \frac{x \sec x^{3} \sin x^{2} \arctan x^{3}-x^{6}}{x^{6} \cos x^{2} e^{x^{3}} \tan \left(x^{4} / 2\right)} .
$$

## Solution:

Q-3) Find the minimum and maximum values of $f(x, y, z)=x z-y^{2}$ on the ball $x^{2}+y^{2}+z^{2} \leq 1$. Solution:

Q-4) Find the volume of the region that lies inside the cylinder $x^{2}+(y-R)^{2}=R^{2}$ and the sphere $x^{2}+y^{2}+z^{2}=4 R^{2}$, where $R>0$.

## Solution:

