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Math 302 Complex Analysis II - Homework 1

| 1 | 2 | TOTAL |
| :---: | :---: | :---: |
|  |  |  |
| 10 | 10 | 20 |

Please do not write anything inside the above boxes!
Check that there are 2 questions on your booklet. Write your name on top of every page. Show your work in reasonable detail. A correct answer without proper or too much reasoning may not get any credit.

Q-1) Let $f: U \rightarrow \mathbb{C}$ be a complex valued function of the form $f(z)=u(x, y)+i v(x, y)$, where $U$ is an open region in $\mathbb{C}$. We know that if $f^{\prime}(z)$ exists at every point $z \in U$, then the Cauchy-Riemann equations $u_{x}=v_{y}$ and $u_{y}=-v_{x}$ hold at every point of $U$.

What can you say about the converse of this fact?

## Solution:

Q-2) Find the Laurent expansion of $\operatorname{cosec} z$ around $z=0$.
Solution:

