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Math 302 Complex Analysis II - Homework 2

| 1 | 2 | TOTAL |
| :---: | :---: | :---: |
|  |  |  |
| 10 | 10 | 20 |

Please do not write anything inside the above boxes!
Check that there are 2 questions on your booklet. Write your name on top of every page. Show your work in reasonable detail. A correct answer without proper or too much reasoning may not get any credit.

Q-1) Discuss the convergence of $\sum_{n=0}^{\infty}\binom{2 n+1}{n} x^{n}$, where $x$ is a real number. Find the sum when it exists.

## Solution:

Q-2) Find the sum of $\sum_{n=0}^{\infty} \frac{1}{n^{4}+1}$. In general describe how to find $\sum_{n=0}^{\infty} \frac{1}{n^{2 k}+1}$, where $k$ is a positive integer.

## Solution:

