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Math 302 Complex Analysis II - Homework 6

| 1 | 2 | TOTAL |
| :---: | :---: | :---: |
|  |  |  |
| 10 | 10 | 20 |

Please do not write anything inside the above boxes!
Check that there are 2 questions on your booklet. Write your name on top of every page. Show your work in reasonable detail. A correct answer without proper or too much reasoning may not get any credit.

Q-1) Show that $f(z)=e^{z}-z$ has infinitely many zeros and that each zero is simple. ( $5+5$ points) Solution:

Q-2) Find explicitly a polynomial $P(x, y)$ such that it is harmonic in the unit disc $D$ around the origin and restricts to $x^{3} y^{3}$ on the boundary of $D$. (Note that $x^{3} y^{3}$ is not harmonic anywhere except the origin.)
Show your work in detail.

## Solution:

